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## Dependence of the superconducting transition temperature on the number of cuprate layers in a unit cell of high-temperature superconductors

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New bismuth and thallium high- $T_c$  superconductors<sup>1,2</sup> contain several N (1, 2, 3, ...) quadratic  $CuO_2$  planes forming sheafs between individual layers of thallium oxides. Neighboring  $CuO_2$  layers in the sheafs are separated by Ca(Sr) ions.

The first theoretical investigation of the dependence of  $T_c$  on the number of  $\text{CuO}_2$  layers within a sheaf was carried out by Anderson et al.<sup>3</sup> Birman and  $\text{Lu}^4$  applied the Ginzburg-Landau approximation to new high- $T_c$  superconductors. They determined the upper limit of  $T_c$  equal to 140 K for monolayer and bilayer thallium families. In several works, the dependence on the number of  $\text{CuO}_2$  layers in a unit cell was calculated by using the microscopic formulation of the generalized BCS theory.

Eab and  $Tang^{5,6}$  derived expressions for the critical temperature  $T_c$  of superconductors with N layers on the basis of the Ginzburg-Landau phenomenological model by using energy minimization. Using the experimental values of  $T_c$  for the first members of a series, the values of  $T_c$  for other members can be determined.

The theory of layered crystals with any number of interacting layers within a unit cell was developed by Jha<sup>7</sup> (see also Refs. 8 and 9).

In all works, it was shown that the value of  $T_c$  increases monotonically with the number of layers in sheafs and attains a constant value for N>10. However, experiments carried out in 1989 by Kikuchi et al. <sup>10</sup> revealed that this is not true. The authors of Ref. 10 synthesized the superconductor  $Tl_1Ba_2CaCu_4O_{12}$  and observed a decrease in the value of  $T_c$  upon a transition from three to four layers. They also synthesized a series of superconductors  $Tl_1Ba_2Ca_{N-1}Cu_NO_{2N+3}$  with the number N varying from two to five  $T_c$ 0 and proved that the value of  $T_c$ 1 increases with  $T_c$ 1 to  $T_c$ 2 and then decreases for  $T_c$ 3.

It was noted in Ref. 11 that such a decrease is also observed for N=6.

In the next sections, we shall explain the experimentally observed decrease in  $T_c$  for large values of N by using the bisoliton model developed at the Institute of Theoretical Physics of the Academy of Sciences of the Ukraine. <sup>12,15</sup>

## 1. ROLE OF INTERPLANE INTERACTION IN HIGH-TEMPERATURE SUPERCONDUCTIVITY

The bisoliton condensate of thallium and bismuth high- $T_c$  superconductors are usually investigated theoretically under the assumption that the value of  $T_c$  is determined only by  $\text{CuO}_2$  planes.

Let us suppose that a unit cell contains N quadratic CuO<sub>2</sub> planes. The energy of quasiparticle pairs forming the bisoliton condensate as a result of interaction of quasiparticles with longitudinal  $\beta_{nx}$  (along the layers) and transverse  $\xi_{n\alpha}$  displacements of the sites  $a_{n\alpha}$  in a crystal is characterized by the Hamiltonian 14.15

$$\mathcal{H} = \sum_{\alpha} \Phi_{n\alpha} \left\{ -J \left\{ \phi_{n+1, \alpha} + \phi_{n-1, \alpha} \right\} \right. \\
+ \left[ W_{\perp} + W_{\parallel} + 2\sigma_{\parallel} \left( \beta_{n+1, \alpha} - \beta_{n\alpha} \right) \phi_{n\alpha} \right. \\
- \mathcal{L} \left\{ \phi_{n, \alpha+1} + \phi_{n, \alpha-1} + 2\sigma_{\perp} \left( \xi_{n\alpha} - \xi_{n\alpha+1} \right) \phi_{n, \alpha+1} \right. \\
+ \left. \left\{ \xi_{\alpha\alpha} - \xi_{n, \alpha-1} \right\} \phi_{n, \alpha-1} \right\} \right\}.$$
(1)

The index  $\alpha=1, 2, ...$  labels the layers in a unit cell. The index n varies from 1 to L. The functions  $\varphi_{n\alpha}$  satisfy the periodic

$$\varphi_{n\alpha} = \varphi_{n+L,\alpha}$$
 (2a)

and the boundary conditions

$$\varphi_{n0} = \varphi_{n, N+1} = 0.$$
 (2b)

The normalization condition

$$\sum_{n=1}^{L} \sum_{n=1}^{N} \varphi_{n\alpha}^2 = 1 \tag{3}$$

indicates that each sheaf of N layers contains a bisoliton.

We shall seek the wave function of a sheaf containing N planes in the form

$$\psi(\xi) = \sum_{\alpha=1}^{N} C_{\alpha} \bar{\varphi}_{\alpha}(\xi) \tag{4}$$

with the coefficients  $C_{\alpha}$  satisfying the conditions

$$C_0 = C_{N+1} = 0; \quad \sum_{n=1}^{N} C_n^2 = 1.$$
 (5)

The energy  $E_{\rm bs}^{(N)}$  of a sheaf containing N layers is defined by the system of equations obtained in Refs. 14, 15:

$$\chi(N) C_{\alpha} - \gamma [C_{\alpha+1} + C_{\alpha+1}] - \sigma [C_{\alpha+1}^2 + C_{\alpha-1}^2] = 0, \tag{6}$$

where

$$\chi(N) = \mathcal{E}_{bs}(N) - \mathcal{E}_{bs}^{0}. \tag{7}$$

The second term in Eq. (6) accounts for the interaction between two adjacent  $CuO_2$  planes separated by Ca(Sr) ions. The third term takes into account the role of variation of interplane distances.

If a unit cell contains only one  $CuO_2$  layer, we must put  $\gamma = \sigma = 0$  in Eq. (6).

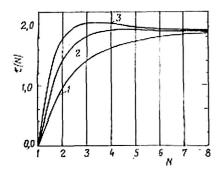


FIG. 1. Dependence of the ratio  $t(N) = [T_c(N) - T_c(1)] d\gamma$  for the values  $\sigma/\gamma = 0$  (1), 0.06 (2), and 0.8 (3) on the number N of plane CuO<sub>2</sub> layers in unit cells of layered superconductors.

### 2. ENERGY OF SHEAFS OF CuO<sub>2</sub> PLANES FOR A FIXED SEPARATION BETWEEN THE PLANES

If we disregard the variation of the separation between the planes in sheafs, we must put  $\sigma = 0$ . In this cse, Eq. (6) is reduced to

$$x(N) C_{\alpha} - \gamma [C_{\alpha+1} - C_{\alpha-1}] = 0$$
 (8)

under the additional conditions (5). Then the energy level  $\mathcal{E}_s^0$  of a plane splits into N sublevels due to the interaction between the layers. The roots of the equation have the following values:

$$\chi_J(N) = -2\gamma \cos[\pi J/(N+1)], \quad J = 1, N.$$
 (9)

The energy is given by

$$\mathcal{E}_{bs}^{(J)} = \mathcal{E}_{bs}^{0} - 2\gamma \cos \left[\pi J/(N+1)\right], \tag{10}$$

where  $\mathcal{E}_{bs}^{0}$  is the energy of a layer. The superconducting state is determined by the minimum value, i.e., for J. Consequently, the critical temperature  $T_c$  of a layered superconductor is defined as

$$T_c(N) = T_c(1) = 2\gamma A \cos \frac{\pi}{N+1},$$
 (11)

where  $T_c(1)$  is the critical temperature of a superconductor with a single plane. The coefficient A can be determined from experimental values for the first members of the series.

#### 3. ENERGY OF A SHEAF OF CuO<sub>2</sub> PLANES WITH A VARYING SEPARATION

In order to calculate the energy of a sheaf of CuO<sub>2</sub> planes taking into account the variation of the separation between the planes, we shall, in the first approximation, make the following substitution in Eq. (6):

$$C_{n+1}^2 + C_{n-1}^2 \to D(N).$$
 (12)

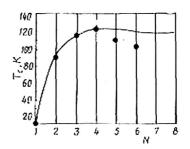


FIG. 2. Theoretical dependence (for  $\sigma/\gamma = 0.6$ ) of the critical temperature  $T_c$  of a series of superconductors  $\text{Tl}_1\text{Ba}_2\text{Ca}_{N-1}\text{Cu}_N\text{O}_{2N+3}$  on the number N of plane layers in unit cells. Experimental data are marked by circles.

In this case, the system of equations (6) is transformed to

$$\{\chi(N) - \sigma D(N)\} C_{\alpha} - \gamma \{C_{\alpha+1} - C_{\alpha-1}\} = 0.$$
 (13)

For a further simplification of our analysis, we shall estimate the functions D(N) by using the values of  $C_{\alpha}$  obtained in Sec. 2 for  $\sigma$ .

The critical temperature of a superconductor containing N layers is defined as

$$\tau(N) = \frac{T_c(N) - T_c(1)}{\gamma A} = 2\cos\frac{\pi}{M+1} + \frac{\sigma}{\gamma} D(N). \tag{14}$$

Figure 1 shows the  $\tau(N)$  dependence for the values of  $\sigma/\gamma$  equal to 0; 0.06 and 0.8. The maximum appears on the  $\tau(N)$  curve when the variation of separation between the planes is taken into account.

Using the experimental values of  $T_c(N)$  for a series of  $TI_1Ba_2Ca_{N-1}Cu_NO_{2N+3}$  superconductors, we can determined the theoretical dependence of  $T_c$  on the number of  $CuO_2$  layers in a unit cell for  $\sigma/\gamma=0.6$ . This dependence is presented by the curve in Fig. 2. Experimental results are indicated by circles.

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